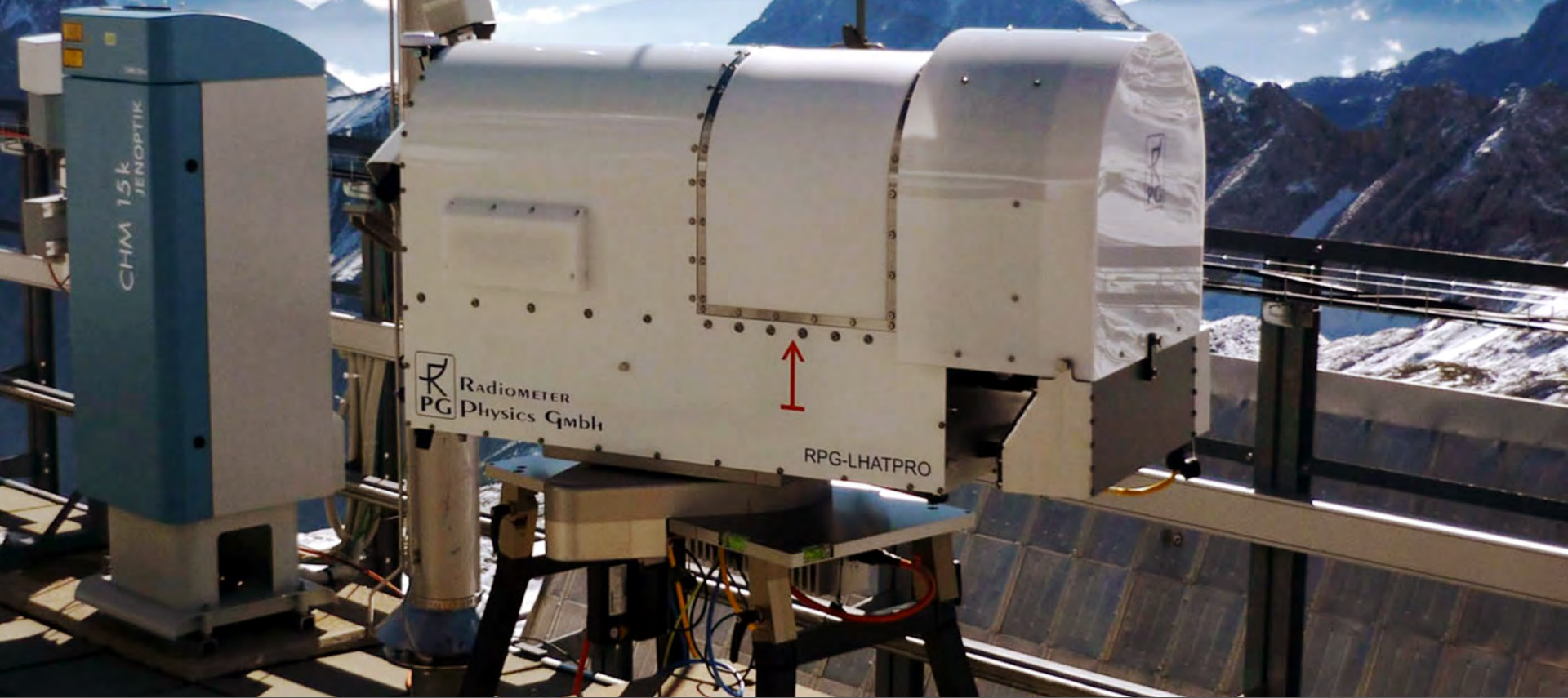




# Microwave Radiometry for Atmospheric Remote Sensing



**Harald Czekala, Thomas Rose, Gerrit Maschwitz**  
RPG Radiometer Physics GmbH, Meckenheim, Germany

1. Intro
2. Nature/Source of observed signal (thermal radiation, TB)
  - Planck's law
  - Conversion of energy units to brightness temperature TB
3. Link between MW spectrum and atmospheric state
  - Absorption lines, transmission windows, information content
4. Measurement devices, radiometer technology
  - Heterodyne + Direct Detection
  - Calibration
5. Retrieval of atmospheric data from microwave data
  - Formulation of the problem
  - Adding instrument imperfection
  - Simulation of the MW data by RTM
  - Regression or iterative
6. Examples...

## What is „Remote Sensing“?

- Observing radiation (more general: energy) reaching a „receiver“ device to learn something about a remote object

*Examples:*

- The human eye  
(binocular total power receiver, multi-pixel focal-plane array, recording of mostly back-scattered light in the 500 nm to 800 nm region...)
- Radar, Lidar, Sonar, Sodar, ....
- IR fever thermometer...
- Microwave spectrometers
- Microwave radiometers

## What are we focussing on? Microwave Radiometry...

- Passive total power radiometers in the centimeter to millimeter wavelength regime (10 GHz to 300 GHz)
- Retrieval algorithms to invert observed microwave sky brightness into something meteorological (meaningful) data



# Basic Concept in one Slide

- **Passive:** detection of microwave **Thermal Radiation** (no power emitted by MWR!)
  - Emission (+absorption, scattering) from atmospheric components:
  - Gases (H<sub>2</sub>O, O<sub>2</sub>, N<sub>2</sub>,... line emission)
  - Hydrometeors (clouds, precipitation, frequency dependent continuum)

- **Radiometric observation:**  
Intensity (sky brightness) in units of brightness temperatures (TB)
  - At several fixed frequencies
  - At several elevation angles

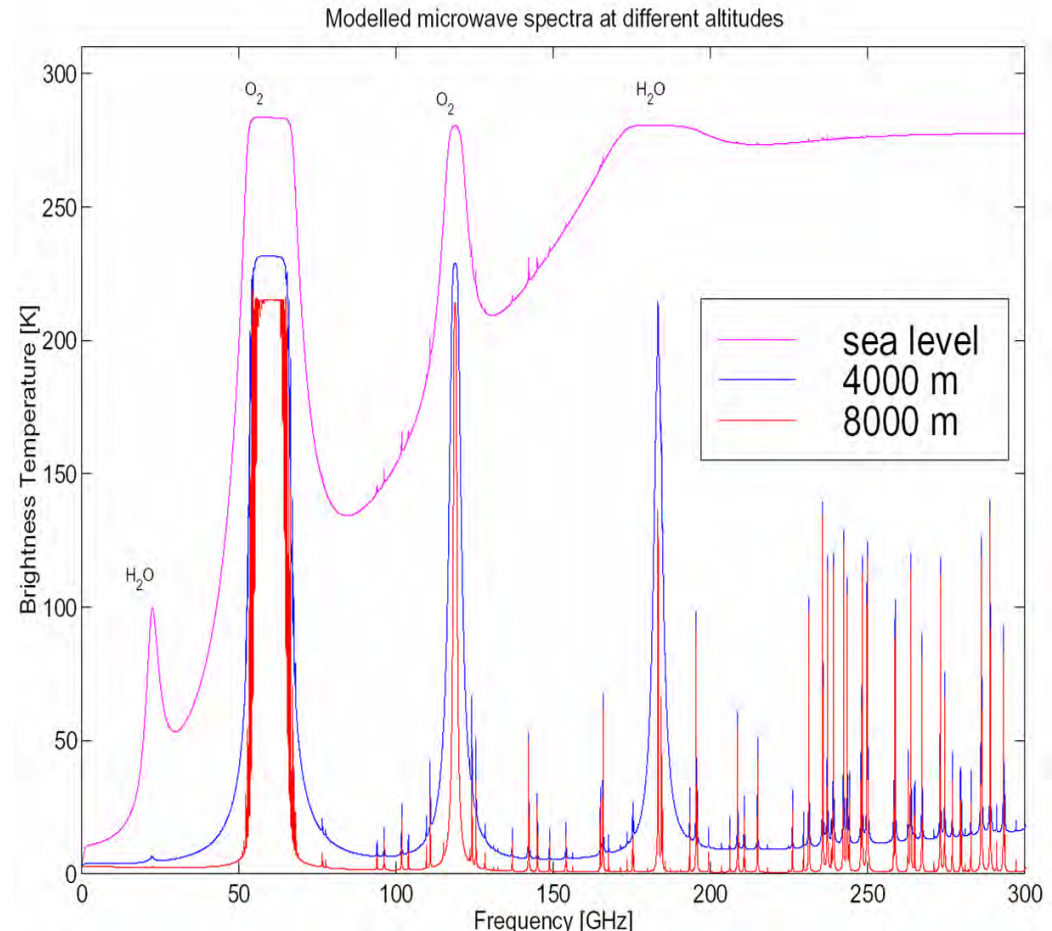
- **Meteorological Variables**  
Calculated by retrievals
  - Solving the „forward problem“ (radiative transfer for a given atmosphere)

$$TB = F(T(z), Q(z), P(z), LWC(z))$$

- Inversion of **F** is the „retrieval“

$$T(z) = F^{-1}(TB)$$

- Inversion problem is ill-posed
- Data set statistics important!



## 2. Thermal Radiation and the Microwave Spectrum

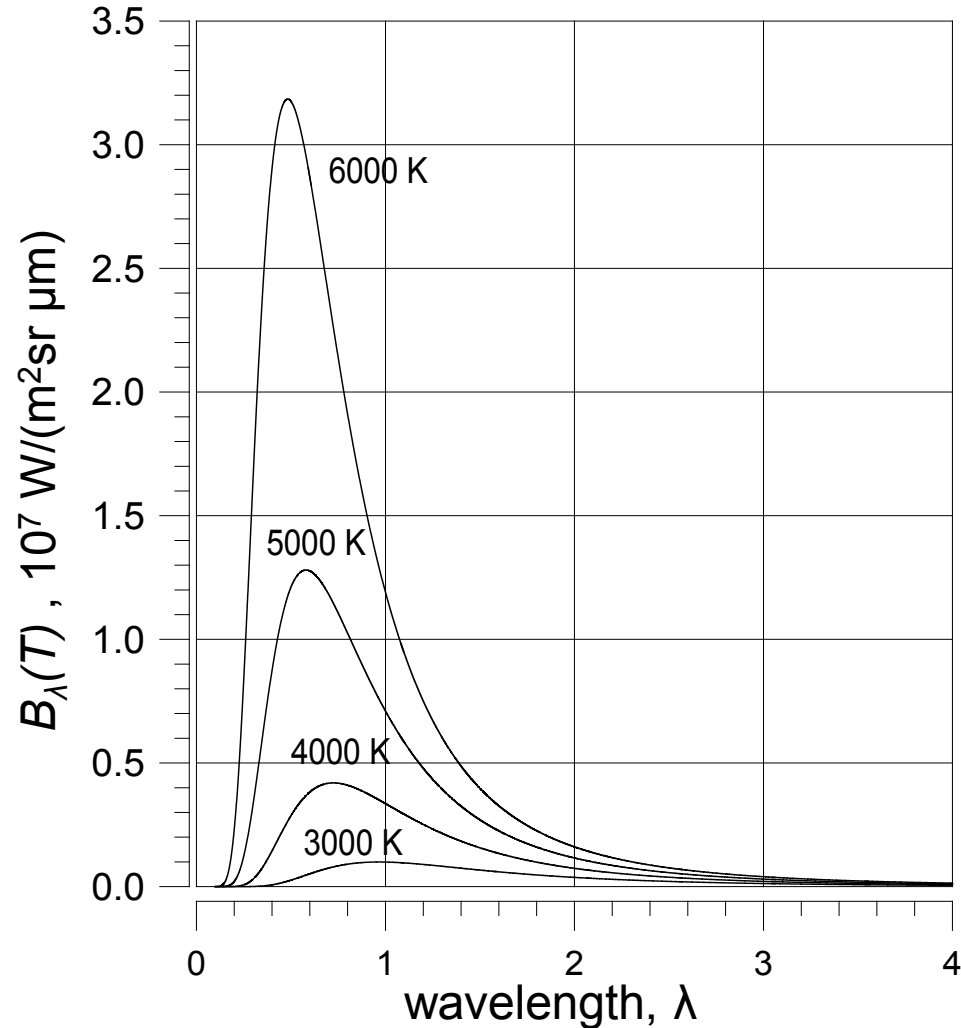
# Thermal Radiation: Planck's Law

- Source of detected signal: Thermal radiation (Planck , 1901)
- All bodies of with  $T > 0$  emit EM radiation at all wavelengths

$B_\lambda$  spectral power density [ $\text{W m}^{-2} \text{sr}^{-1} \text{m}^{-1}$ ]  
 $h = 6.626 \cdot 10^{-34} \text{ J s}$  Planck's constant  
 $k_B = 1.38 \cdot 10^{-23} \text{ J/K}$  Boltzmann const.  
 $c = 2.99792 \cdot 10^8 \text{ m/s}$  speed of light

$$B_\lambda(T) = \frac{2hc^2}{\lambda^5} \frac{1}{\exp\left(\frac{hc}{k_B \lambda T}\right) - 1}$$

$$B_\nu(T) = \frac{2h\nu^3}{c^2} \frac{1}{\exp\left(\frac{h\nu}{k_B T}\right) - 1}$$



# Observables: Intensity → Brightness Temperature

- Radiometers observe „sky brightness“

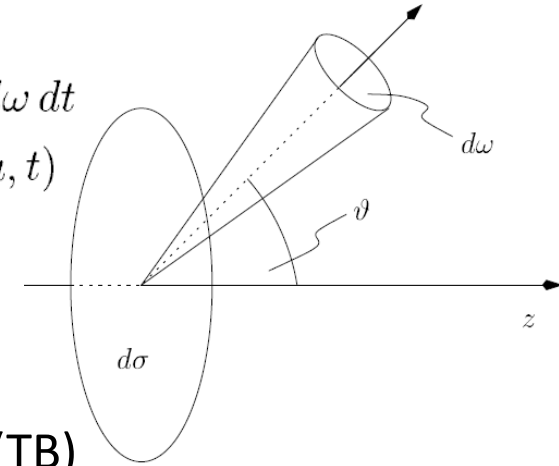
*or: radiant energy*

*or: specific intensity, ...*

$$dE_\nu = I_\nu \cos \theta d\nu d\sigma d\omega dt$$

$$I_\nu \equiv I_\nu(x, y, z, \gamma, \delta, \mu, t)$$

- Units:  $W m^{-2} sr^{-1} Hz^{-1}$
- Extremely small power levels:  $P \sim 10^{-13} W$   
(demands high amplification, 100 dB)
- More „human readable“ units: Brightness Temperature (TB)



The brightness temperature  $T_B$  is defined as the temperature at which the blackbody emission  $B(T_B)$  exactly matches the measured intensity  $I$ :

$$I = B(T_B). \tag{2.9}$$

By inverting Planck's function for a measured intensity one obtains the corresponding brightness temperature

$$T_B = B^{-1}(I). \tag{2.10}$$

- Optically thick (solid) objects have  $TB = \epsilon \cdot (T_{\text{physical}})$  (with emissivity  $\epsilon = 0.0 \dots 1.0$ )
- Optically thin media: translucent, optical thickness  $\tau$  absorption & emission proportional to presence of absorbing matter → **RTM (Radiative Transfer Model)**

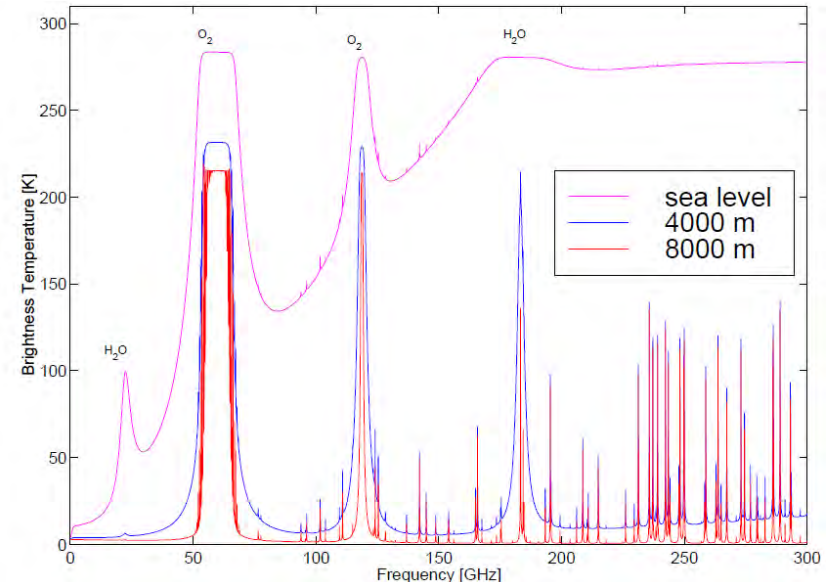
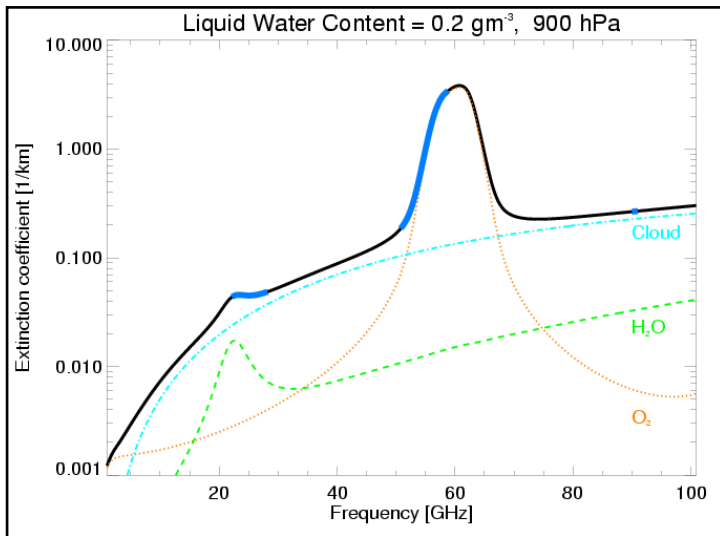
$$\tau = \int_0^\infty \alpha(s) ds$$

## 3. How the MW Spectrum is defined by the Atmosphere



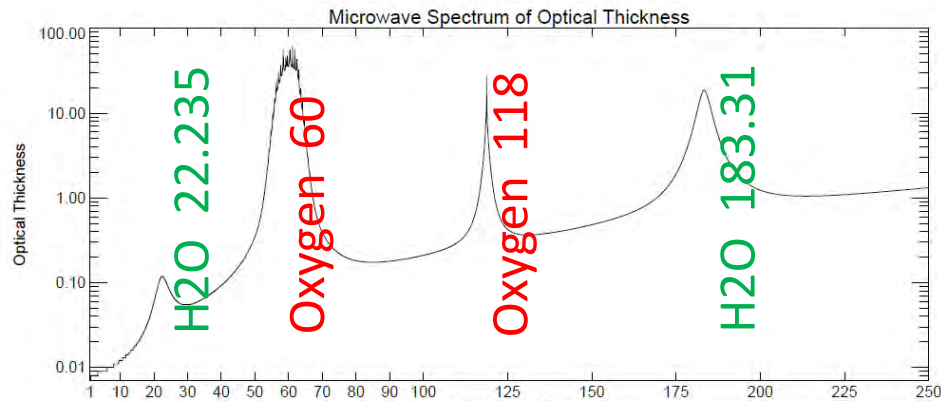
# Impact of Atmosphere on MW Spectrum (I)

- Emission proportional to absorption (**Kirchhoff's** radiation law)
- Atmosphere is made from gas and small particles  
 → **discrete absorption lines** rather than continua (quantum mechanics)
- Atmospheric constituents define the observed spectrum

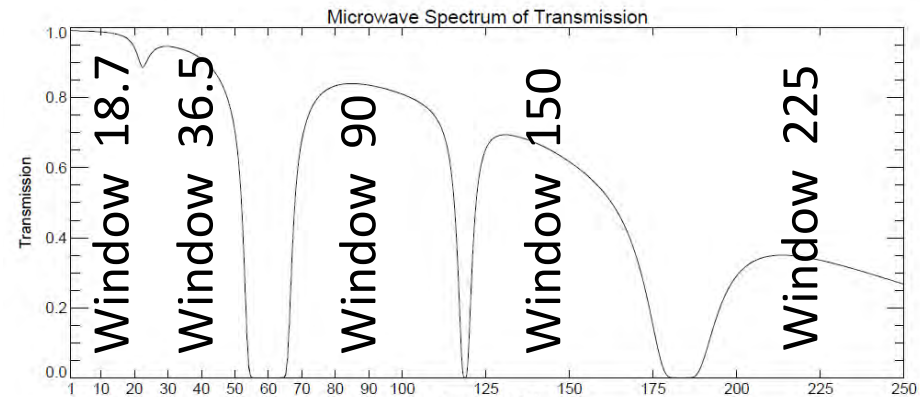


- Emission lines of water vapour (vary with H<sub>2</sub>O Mixing ratio, and Temperature)
- Emission lines of Oxygen (vary with T, but mixing ration is fixed)
- Window channels in between lines: mostly affected by liquid water and the far wings of other lines
- At higher frequencies: trace gases

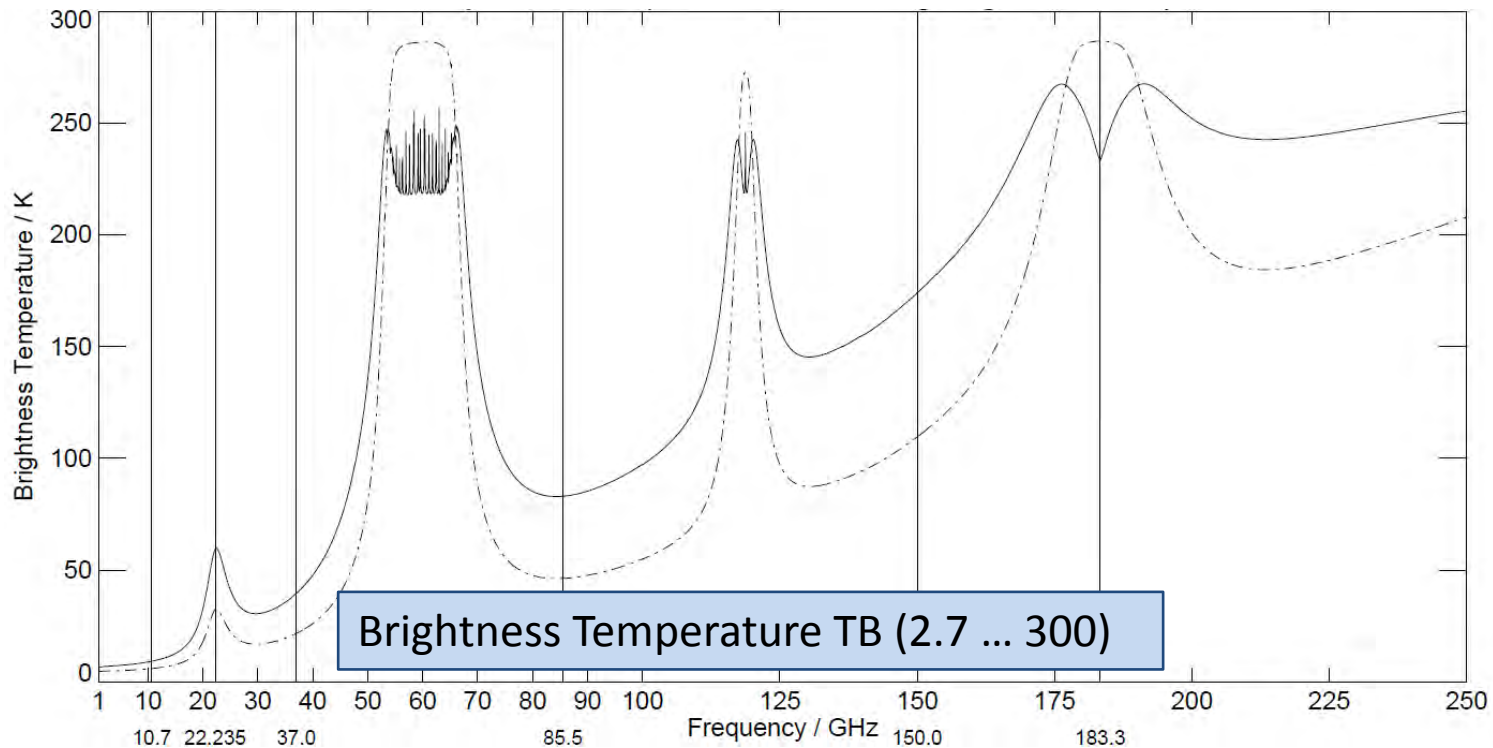
# Different views of the MW Spectrum



Optical thickness (0 ... 100, or more)



Transmission (0 ... 1)



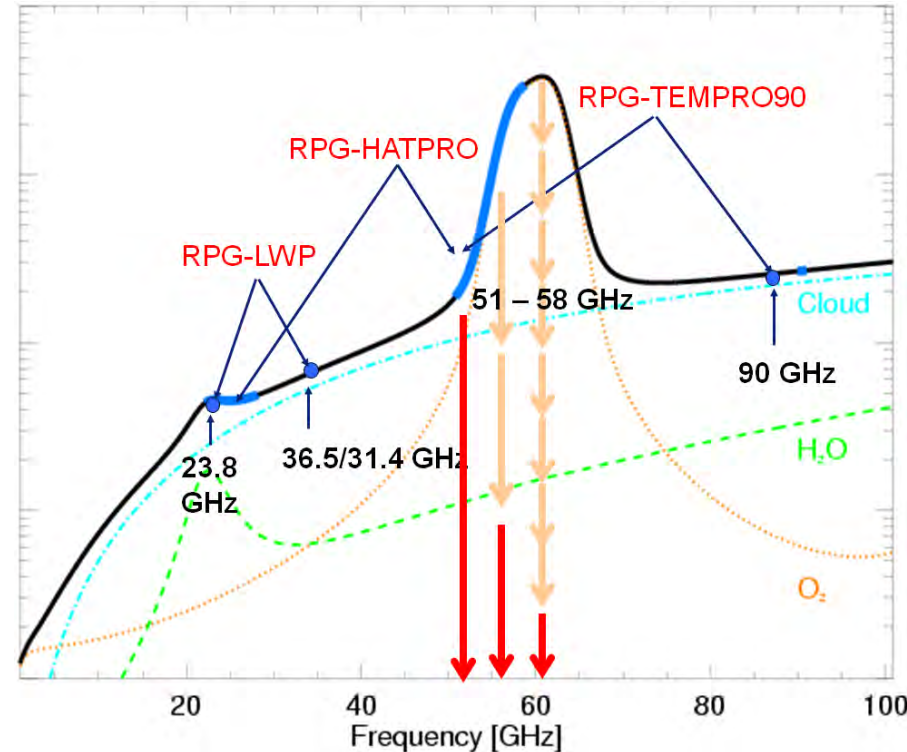
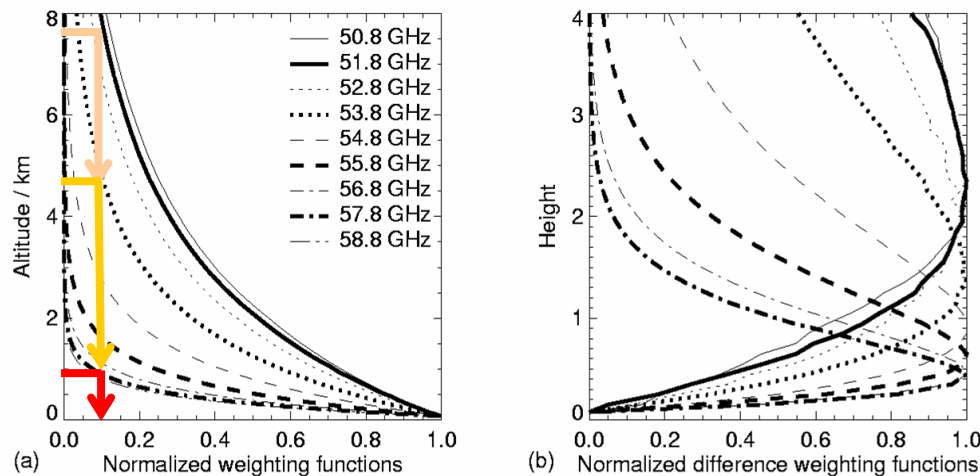
Brightness Temperature TB (2.7 ... 300)

## LWP/IWV:

- Compare a channel in the H<sub>2</sub>O line with a window channel
- Increase in H<sub>2</sub>O increases TB in line, not in the window
- Increase in LWP adds to both channels, (most in the window)

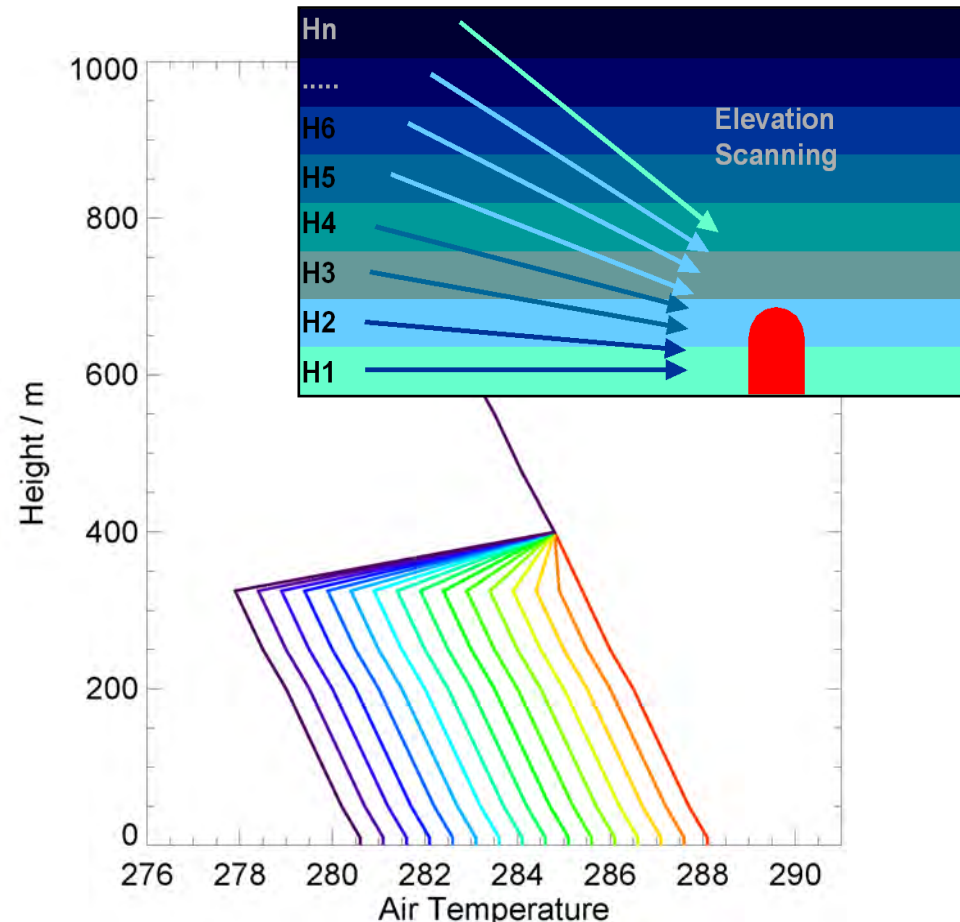
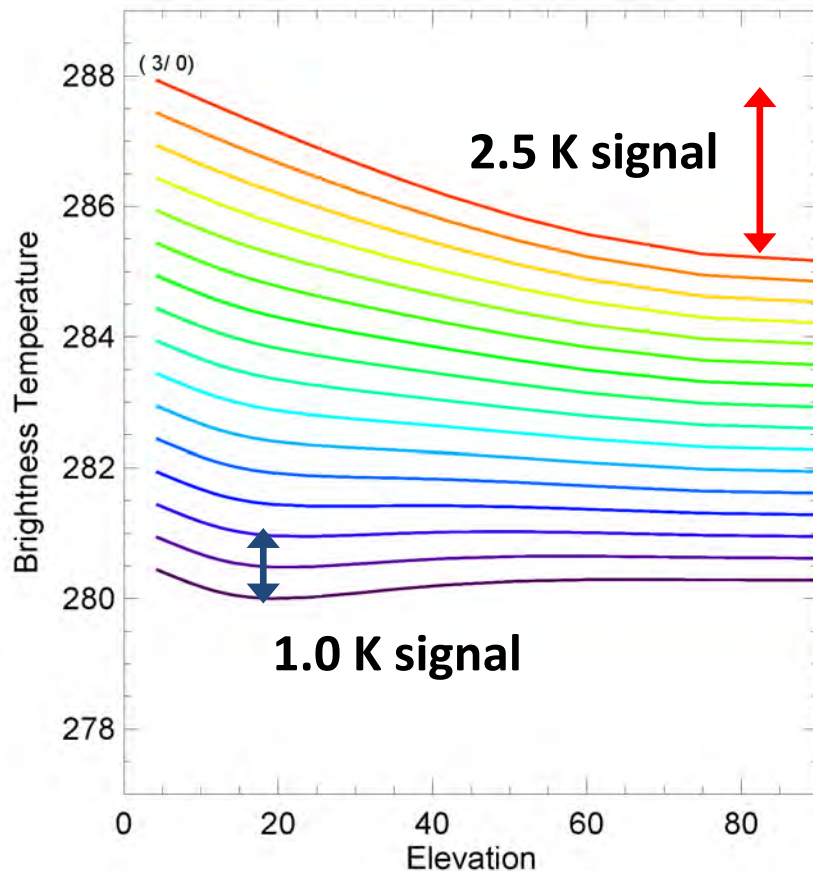
## T-Profile:

- Frequency dependent absorption depth
- Contributions from upper atmosphere to total received signal are stronger for low absorption (absorption on the way down)
- Concept of weighting functions...



## Boundary Layer T-Profile:

- Absorption length decreases for frequencies at line center (60 GHz)
- Limited (approx. 600 m) emission depth @ 58 GHz
- Weighting functions shifted towards surface by elevation scans



## Done so far:

- the source of the radiation, and
- the way the atmospheric conditions make an imprint on the microwave spectrum...

## Remaining:

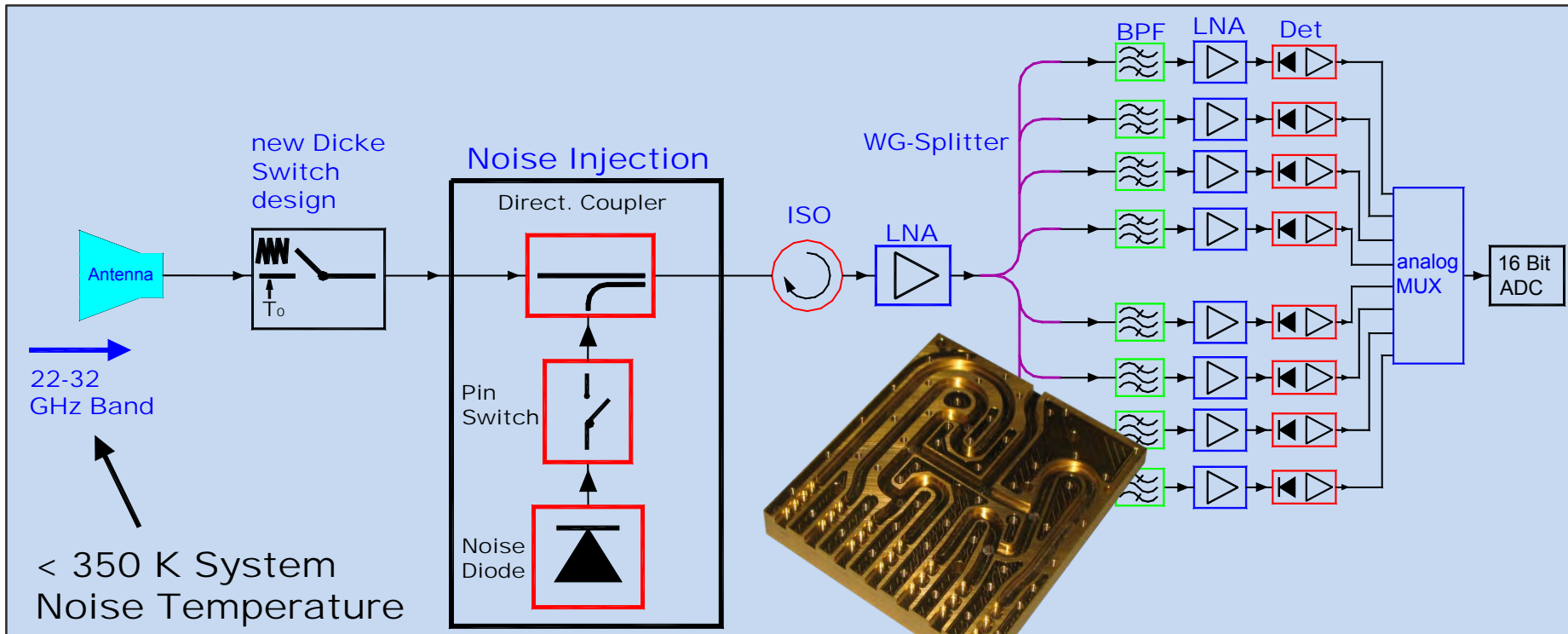
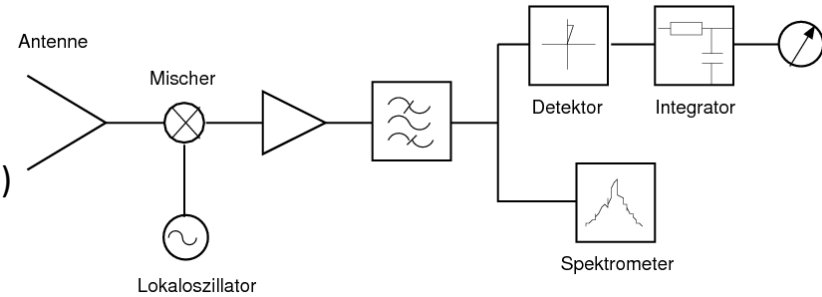
- Have a measurement device for microwave radiation
- Transform microwave measurements into atmospheric data

# 4. Radiometers: Hardware

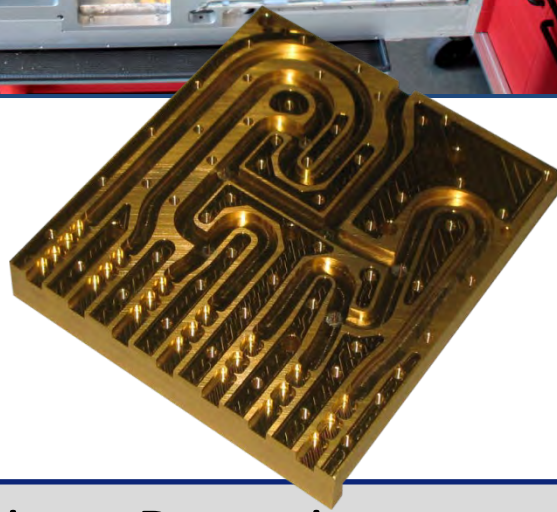
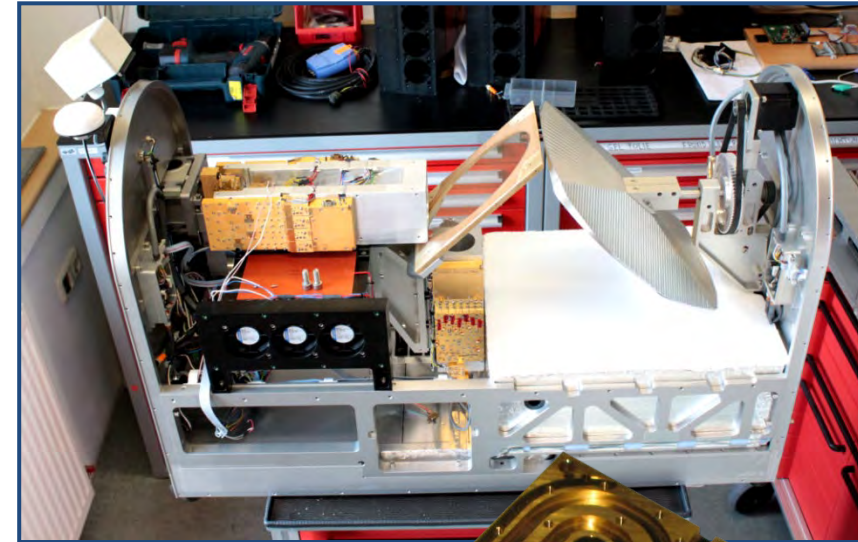


# Radiometer Technology (I): Layout

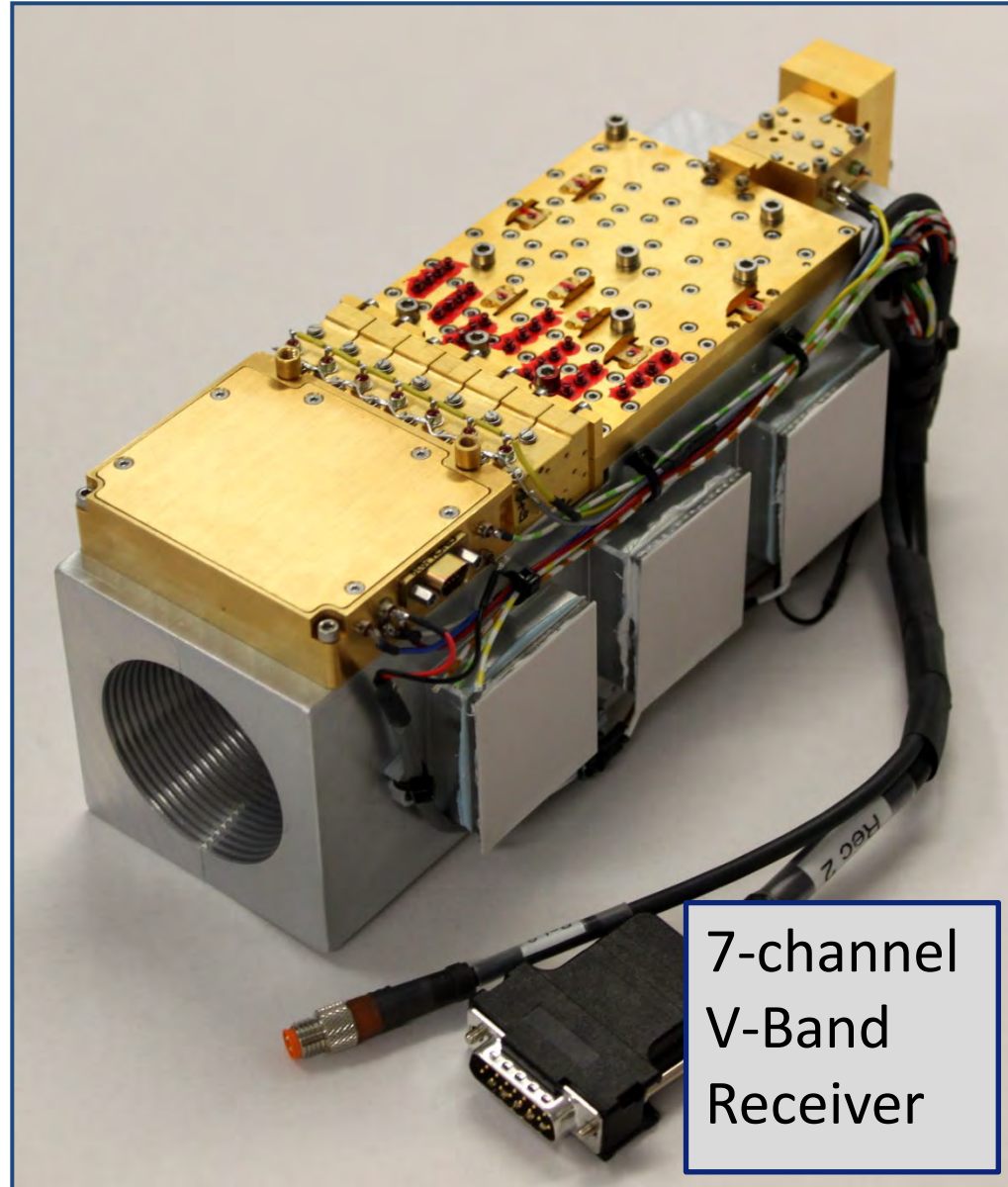
- Select **frequencies** for variables of interest (+  $NE\Delta T$ , bandwidth, ...)
- Select a receiver technology
  - Direct-Detection Filterbank: Amplify, split, filter, detect
  - Heterodyne: down-conversion to IF, the process the IF, or sequentially scan the LO over scppterum (slow, RFI problems)
- Select calibration mechanisms
- Engineer a robust infrastructure around the RF



# Hardware Example



HATPRO Direct Detection  
Filterbank Profiler  
(parallel data acquisition 14 ch.)



7-channel  
V-Band  
Receiver

# Frequencies, bandwidth and # of channels



	K Band (22- 31)	V Band (50-60)
Channel 1	22.24 GHz / 200 MHz	51.26 GHz / 230 MHz
Channel 2	23.04 GHz / 200 MHz	52.28 GHz / 230 MHz
Channel 3	23.84 GHz / 200 MHz	53.86 GHz / 230 MHz
Channel 4	25.44 GHz / 200 MHz	54.94 GHz / 230 MHz
Channel 5	26.24 GHz / 200 MHz	56.66 GHz / 650 MHz
Channel 6	27.84 GHz / 200 MHz	57.30 GHz / 1000 MHz
Channel 7	31.40 GHz / 200 MHz	58.00 GHz / 2000 MHz
Tsys	< 350 K	< 600 K
Degrees of Freedom	2 to max. 3 uncorrelated informations	approx. 5 uncorrelated informations

## Auto-Calibration Devices:

Noise Injection + Magnetically switched Isolators

20 Hz Dicke-Switching, ultra-stable, **4000 s** Allan-Stability

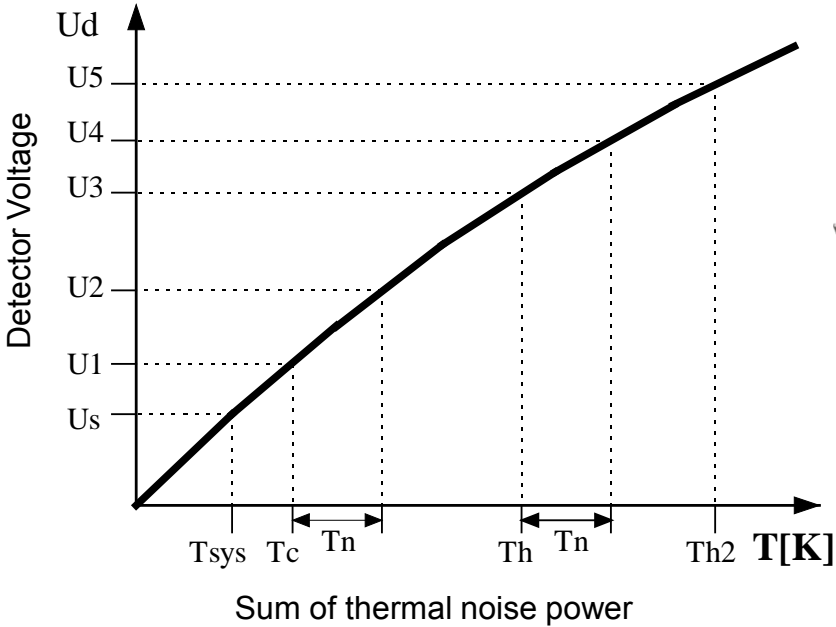


# Radiometer Technology (II): Calibration

- Detector always „sees“ contributions from
  - system emission of lossy components,
  - plus scene (atmosphere signal),
  - plus additional calibration signals
- Voltage signal proportional to second moment of E-field (total power, no phase!)
- $T_{sys}$  describes systems sensitivity limits by own emission:  
 $T_{sys}=3000\text{ K}, T_{sig}=300\text{ K} \rightarrow \text{SNR}=0.1$
- Gain (mV/K): frequently measure G by comparison of TB with black body (quasi-optical load or waveguide termination)

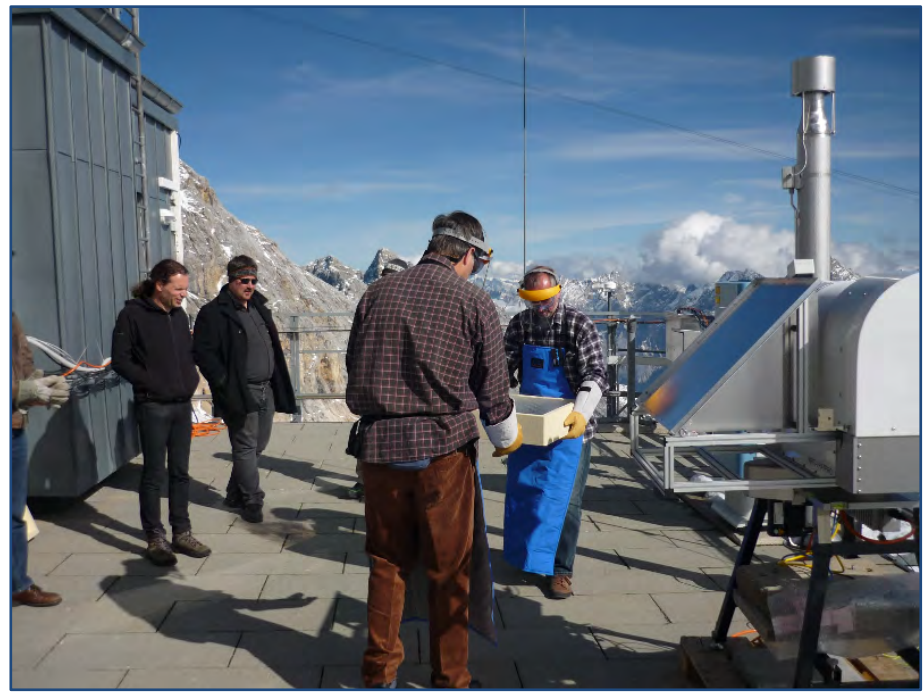
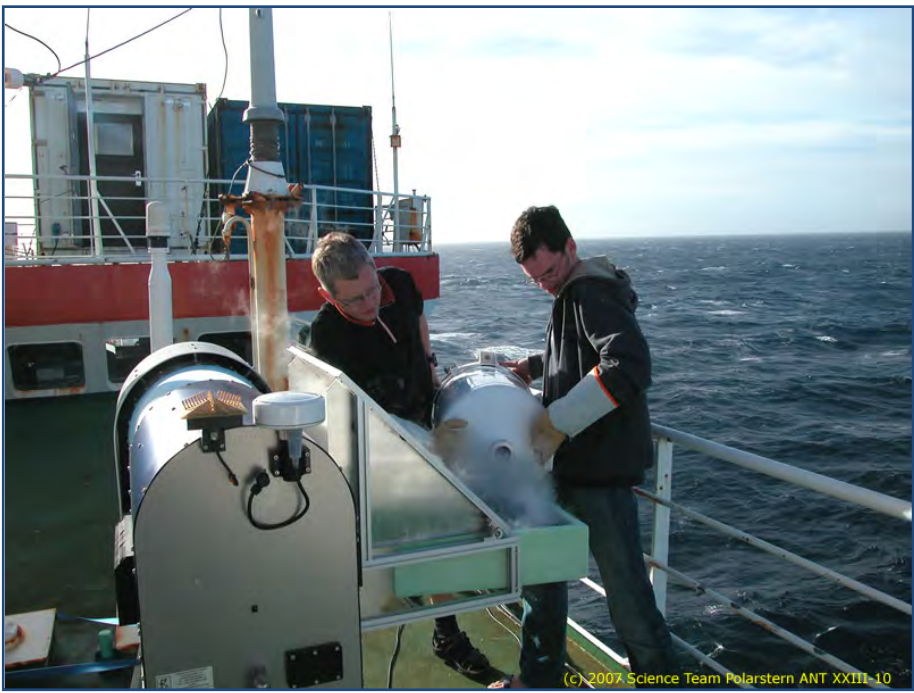
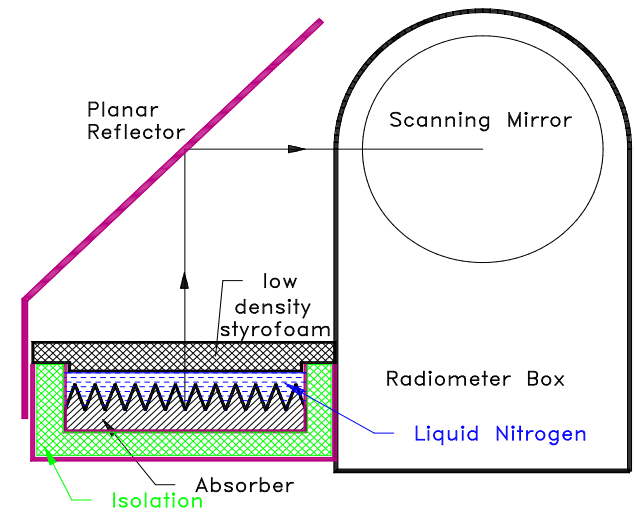
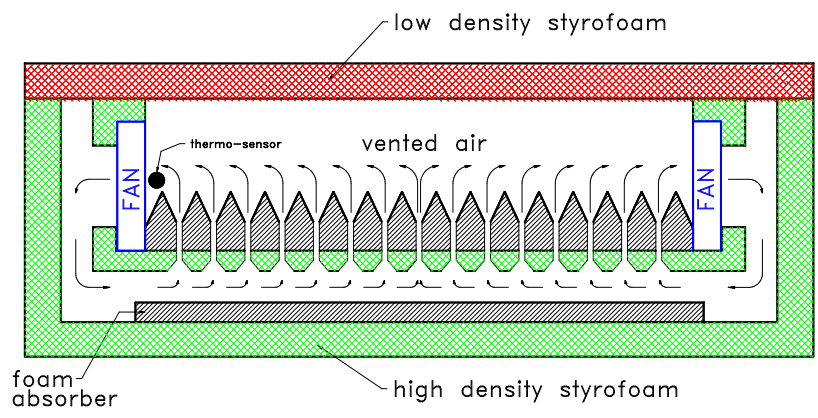
$$\Delta T_B = \frac{T_{sys}}{\sqrt{\Delta \nu \cdot \tau_{int}}}$$

$$U_D = G(T_{sys} + T_{sig})^\alpha, \quad \alpha \leq 1$$



- Initial 4-point Calibration:
- 1) Cold load
  - 2) Cold load + noise diode
  - 3) Ambient load
  - 4) Ambient load + noise diode
- 4 Equations for 4 unknowns  
 → Derive  $G, T_{sys}, T_n, \alpha$

# Radiometer Technology (III): Calibration examples

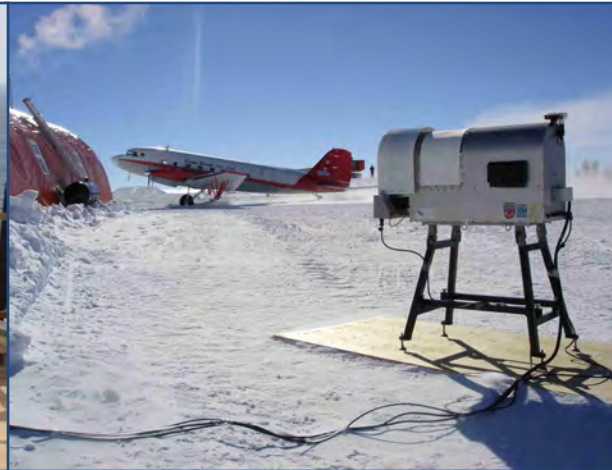




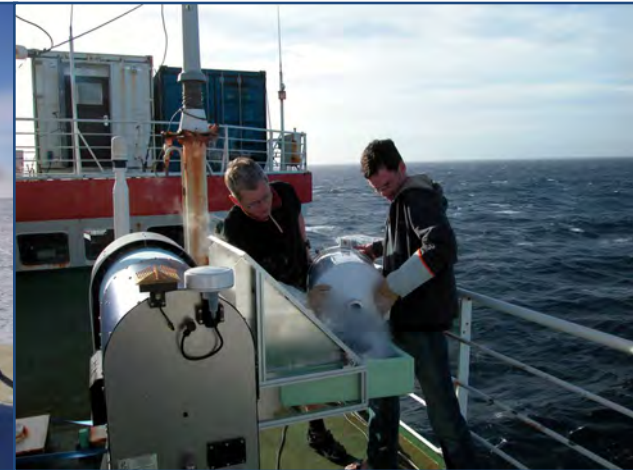
# Challenge: Environment Conditions



Lampedusa, Italy  
(humid, hot, salty)



Dome-C, Antarctica  
(3.300m, -25 to -80 °C)



Research Vessel "Polarstern"  
(Atlantic Ocean)



ALMA site, Chile  
(5.500m above sea level)



Zugspitze, Germany  
(2.800m, -35 °C, 250km/h wind)



AMMA campaign, Benin  
(West-Africa, hot climate, dust)

## 5. How to Retrieve Meteorological Data from TB data

- Solving the „forward problem“ (radiative transfer for a given atmosphere)

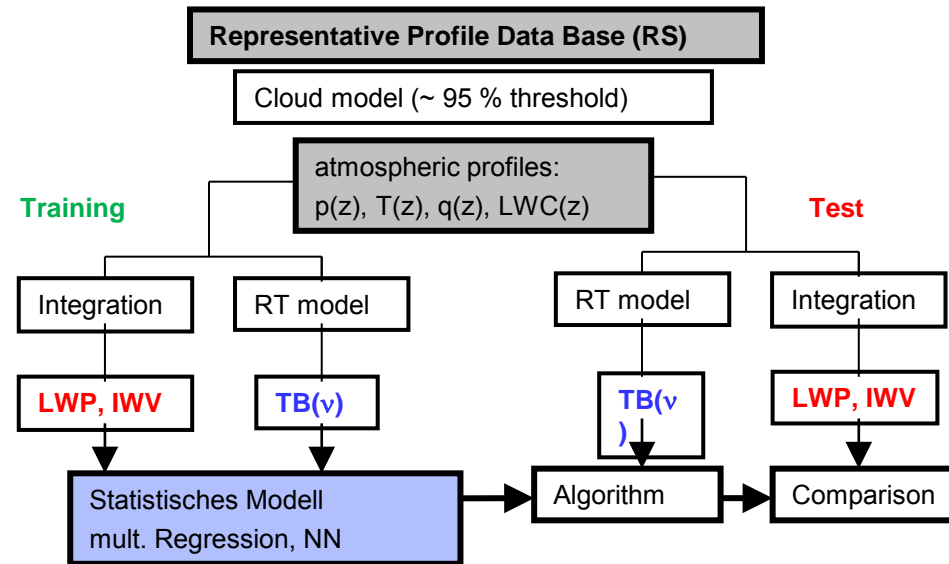
$$TB = F(T(z), Q(z), P(z), LWC(z))$$

- Inversion of **F** is the „retrieval“, e.g.:

$$T(z) = F^{-1}(TB)$$

- Inversion problem is ill-posed
- Data set statistics important!

- Radiative Transfer Model simulates the instrument response to each atmospheric state („Forward Model“)
- Different choices for inversion scheme:
  - Regression retrievals derived by fitting mathematical function to explain atmospheric variables as a function of the TB-vector
  - Iterative („physical“) retrievals start with a first guess state and iteratively modify the profile to minimize the TB difference between simulated and measured TB  
→ 1D-Var, 4D-Var

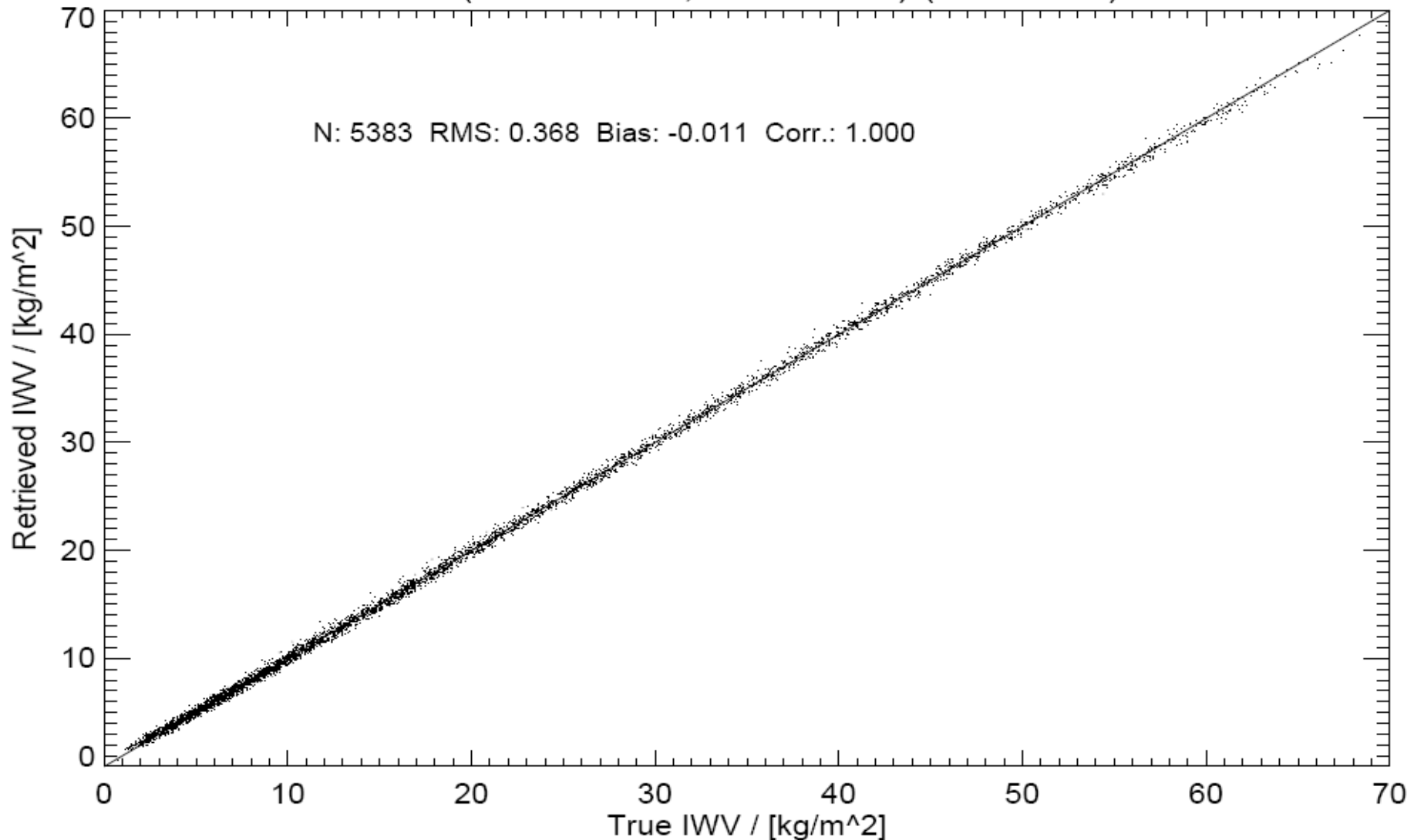


1. **Task:** Find equation that links IWV to brightness temperatures (TB):
 
$$\text{IWV} = a_0 + a_1 \cdot \text{TB}_1 + a_2 \cdot \text{TB}_2 + a_3 \cdot \text{TB}_3 + \dots$$

$$(\text{IWV} = a_0 + a_1 \cdot \text{TB}_1 + a_2 \cdot (\text{TB}_1)^2 + a_3 \cdot \text{TB}_2 + \dots)$$
2. Use 10.000 Radio soundings to
  - Calculate/Analyze **real IWV** from soundings
  - Simulate TB1, TB2, TB3, ...
3. Use 5.000 pairs of IWV and corresponding brightness temperature vectors (TB1, TB2, TB3, ...) to derive coefficients a0, a1, a2, a3, ...
4. Use remaining 5.000 pairs of real IWV and simulated TB to test the retrieval:
  - For each set of simulated brightness temperatures, apply coefficients a0,a1,a2,.. to calculate (=retrieve) a **simulated IWV** (not real TB measurements, but simulated TB measurements used during retrieval)
  - Compare “**real IWV**” to “simulated IWV” from application of retrieval
  - For 5.000 cases, we have a difference of real IWV and retrieved IWV (and can calculate correlation, RMS, Bias)
  - Real IWV is integral of RH-profile
  - Simulated IWV is retrieved from simulated TB-vector, which is depending on the full atmospheric condition (different cloud situations, different T-profiles, etc...)

- Retrieval self test estimates expected performance in terms of RMS

IWV (Filterbank-1, 7 channels) (Test Data)



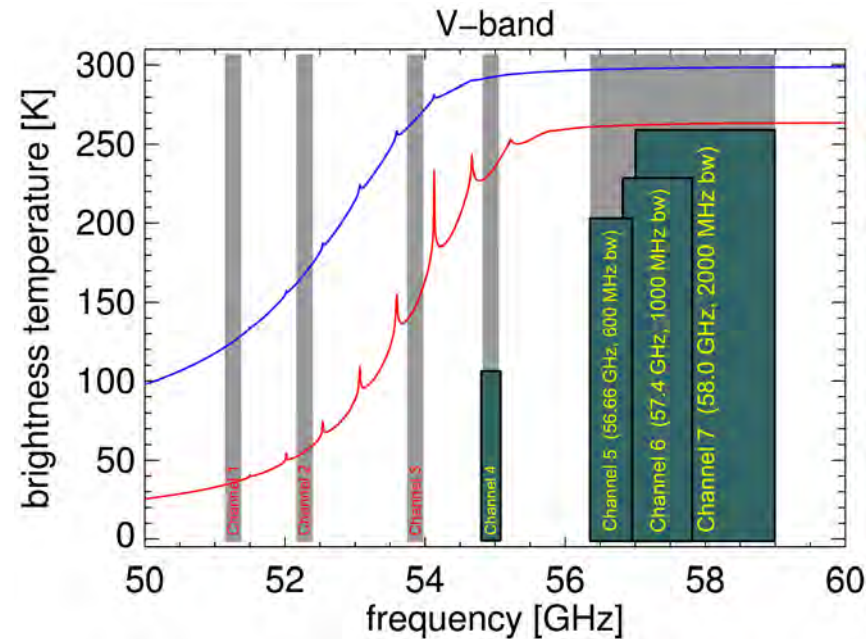
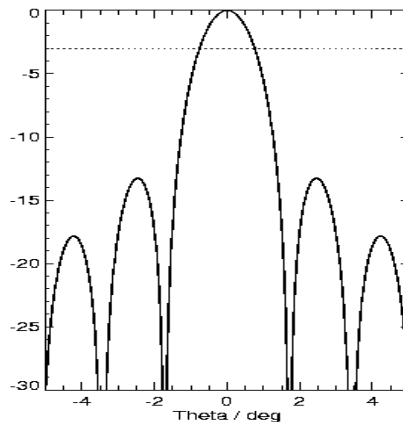
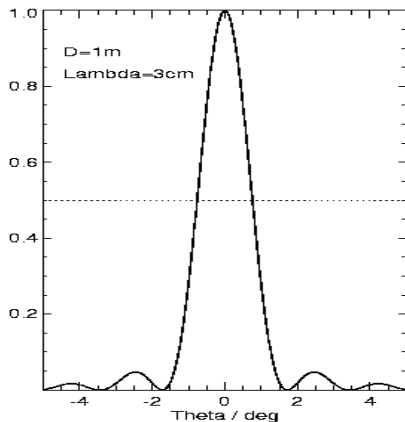


- RT model solves 1D or 3D radiative transfer equation
- Simple emission/absorption models
- Sophisticated (multiple) scattering codes
- Polarization (surface effects, non-spherical hydrometeors)

$$\frac{d\bar{\mathbf{I}}(z, \theta)}{\frac{1}{\mu} dz} = -\bar{\sigma}_e(z, \theta) \bar{\mathbf{I}}(z, \theta) + \bar{\sigma}_a(z, \theta) B(T(z))$$

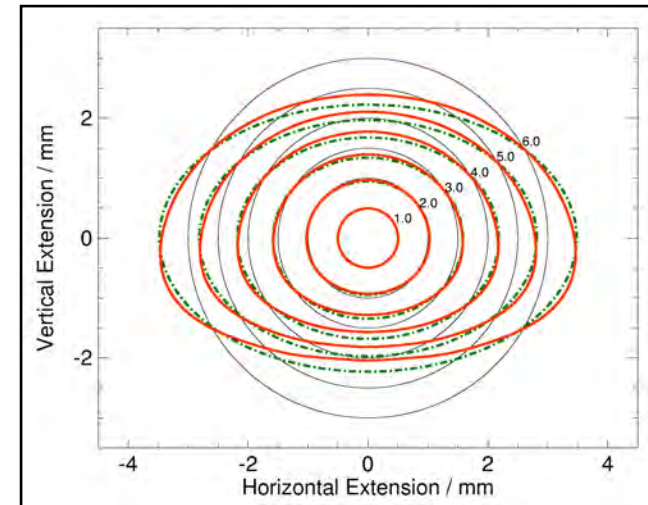
## Before retrieval building:

- Last processing layer needs to model the imperfections of the radiometer system, such as
  - RMS noise
  - Calibration uncertainties
  - Band width effects (no such thing as a centre frequency!)
  - Beam width (antenna patterns usually 1 to 10 degree)
  - Earth curvature (transparent channels)



# RTM Model (continued)

- Simplified (non-scattering) RT model only good for non raining atmospheres
- Scattering more important at higher frequencies
- At low frequencies: Polarization effects by emission of non-spherical particles (rain at 10 GHz)
- Extension for rain or snow (graupel, ice, ...):
  - Polarized RTE using the 4-component Stokes vector
  - 4 coupled Integro-Differential equations (with boundary conditions)

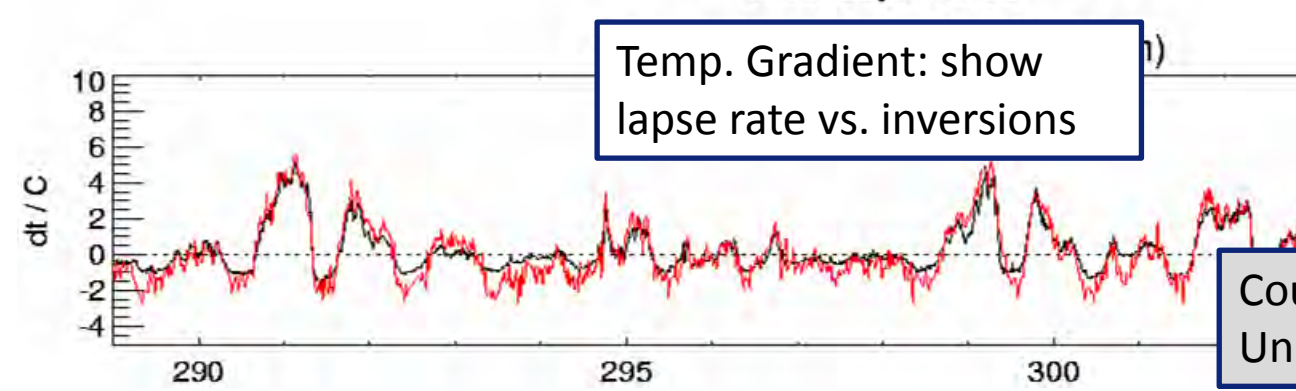
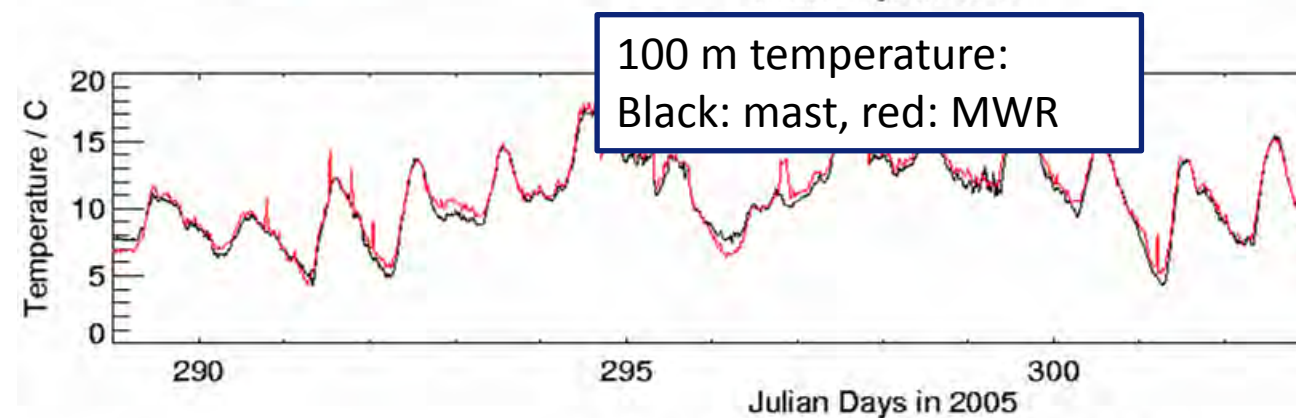
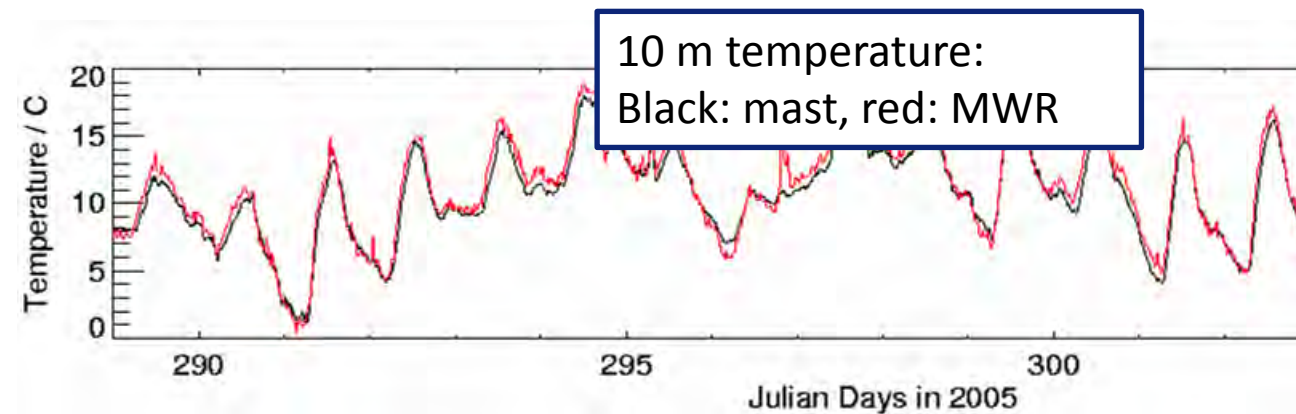


## Differential change

$$\frac{d\bar{\mathbf{I}}(z, \theta)}{\frac{1}{\mu} dz} = - \underbrace{\bar{\sigma}_e(z, \theta) \bar{\mathbf{I}}(z, \theta)}_{\text{Extinction loss (absorption + scattering)}} + \underbrace{\bar{\sigma}_a(z, \theta) B(T(z))}_{\text{Emission source}} + \underbrace{\int_0^\pi \bar{\mathbf{P}}(z, \theta; \theta') \bar{\mathbf{I}}(z, \theta') \sin \theta' d\theta'}_{\text{Scattering source (phase function)}}$$

## 6. Data Examples

# Comparison with Mast data: 15 day time series

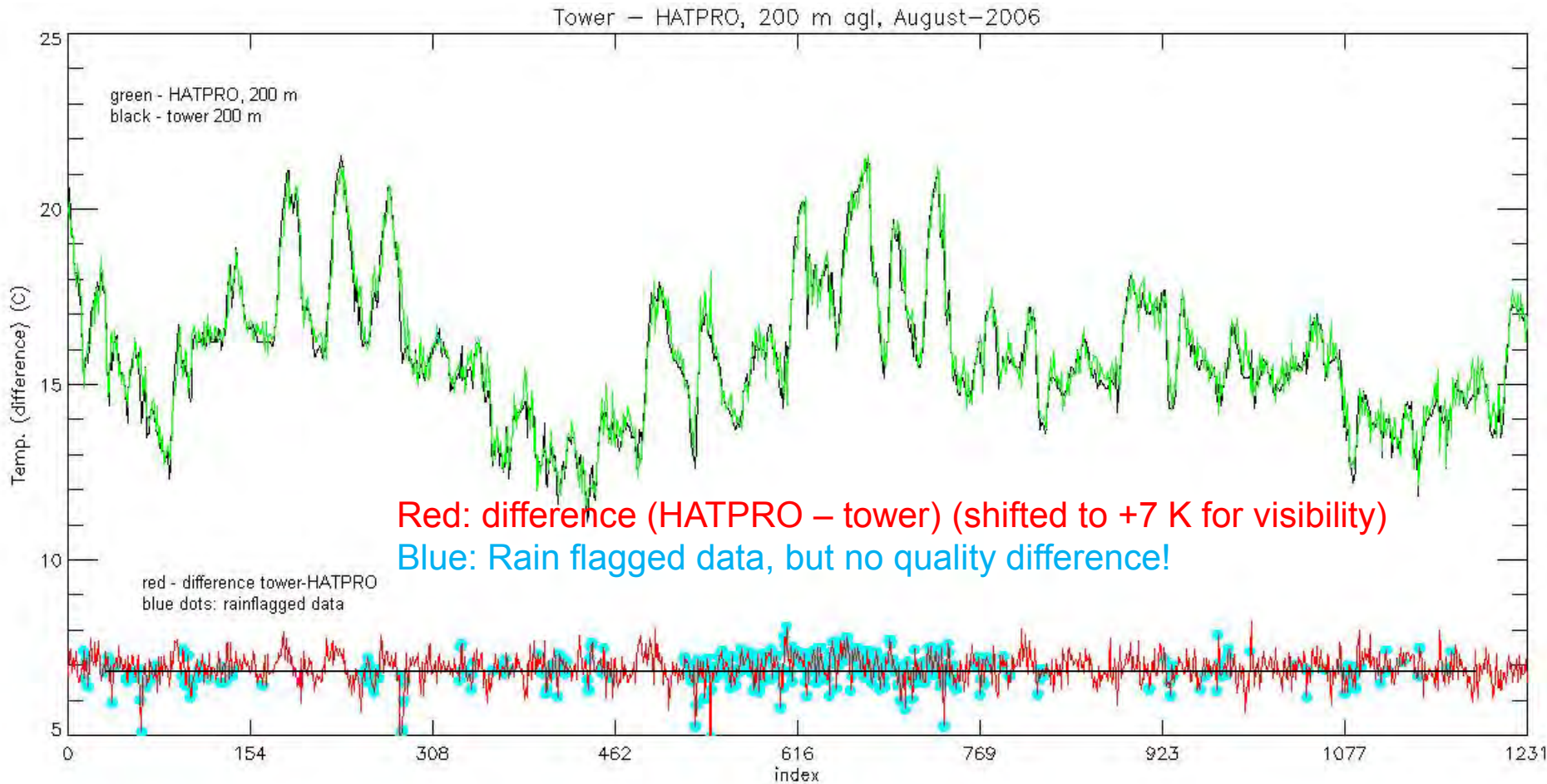


Courtesy of Susanne Crewell,  
University of Cologne, Germany



# Measurements: 200m temperature at KNMI mast

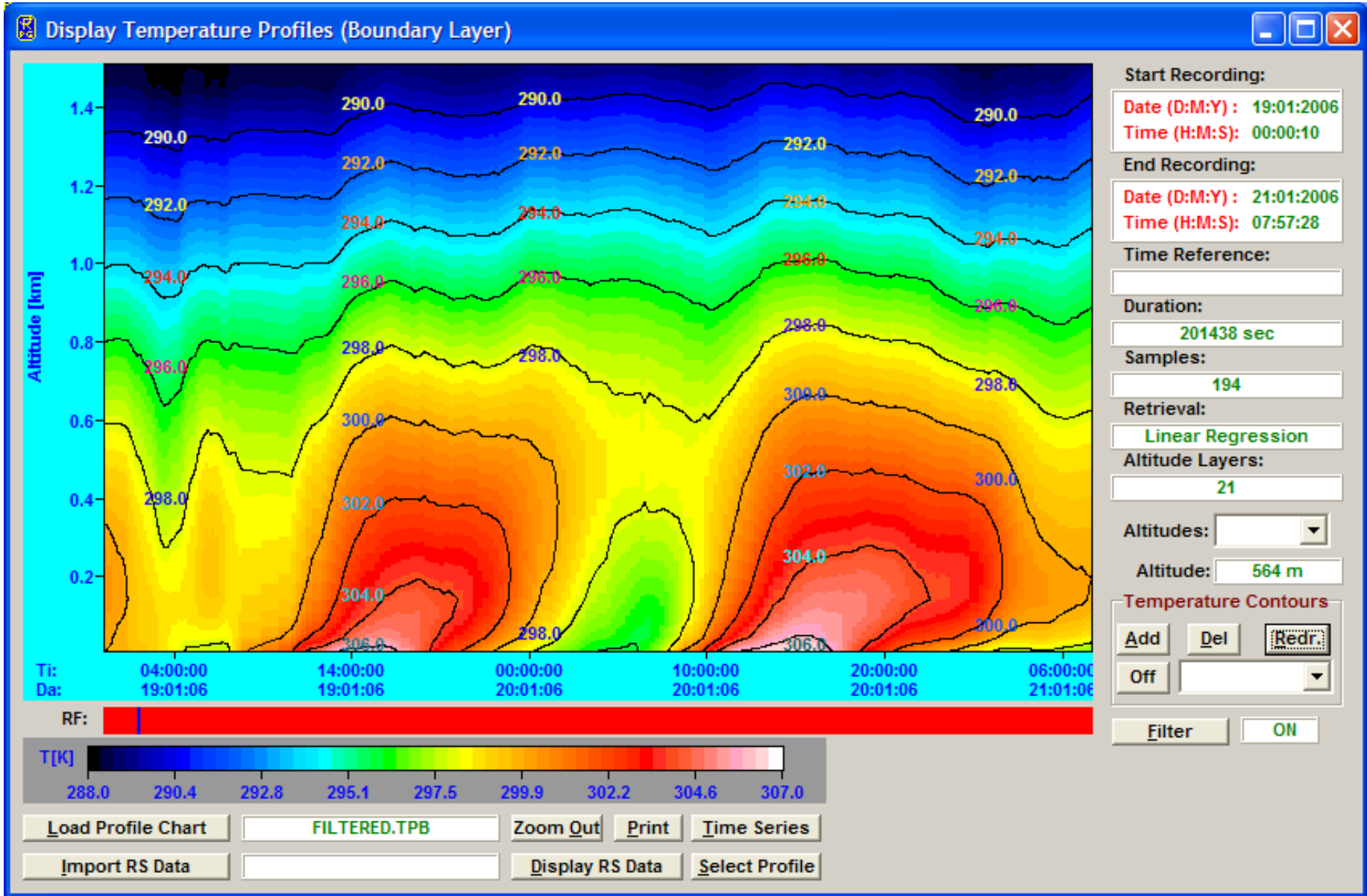
- Comparison of HATPRO 200m temperature measurements with tower at 200m
- **RPG-Boundary-Layer-Mode:** elevation scans, optimized bandpass filters, small beam

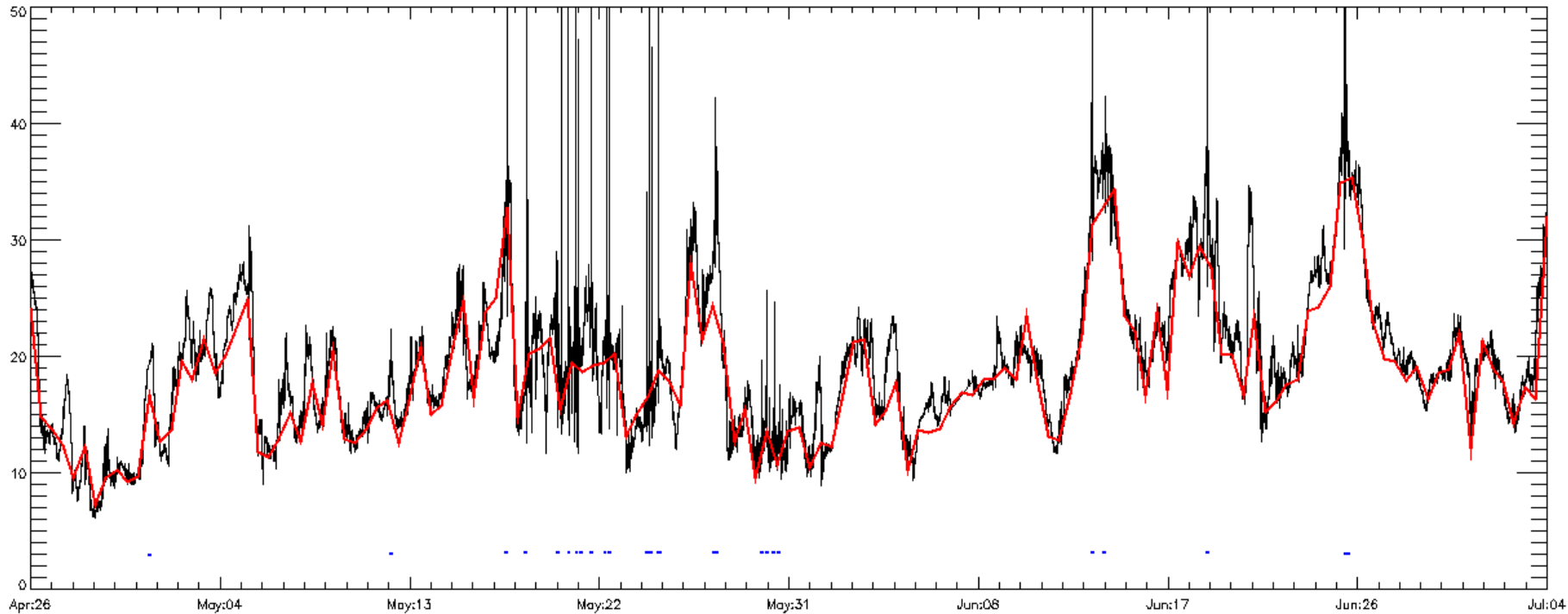


Courtesy of Henk Klein-Baltink, KNMI, Neatherlands



# Boundary Layer temperature profile



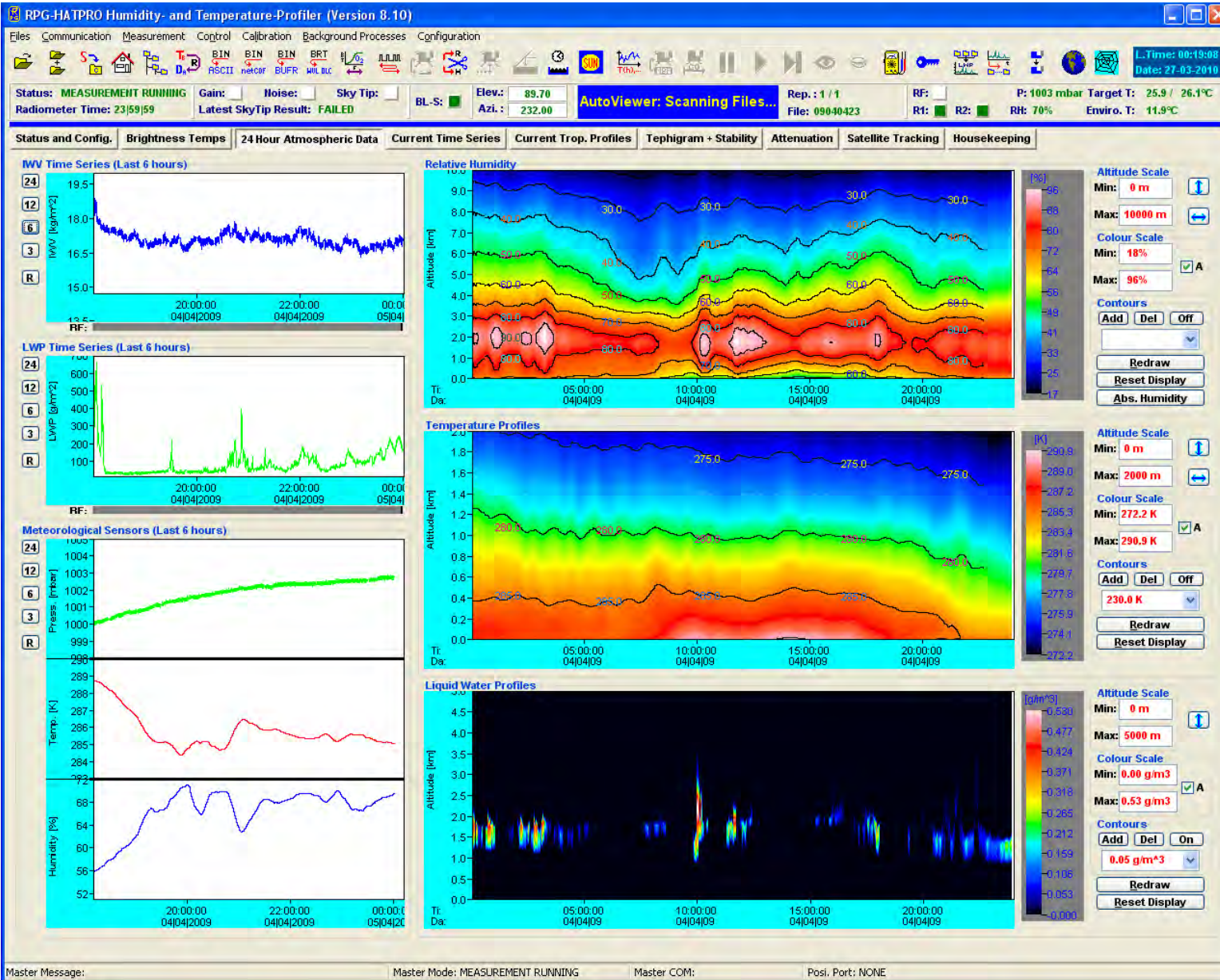


IWV time series over one month (KNMI, May 2006).

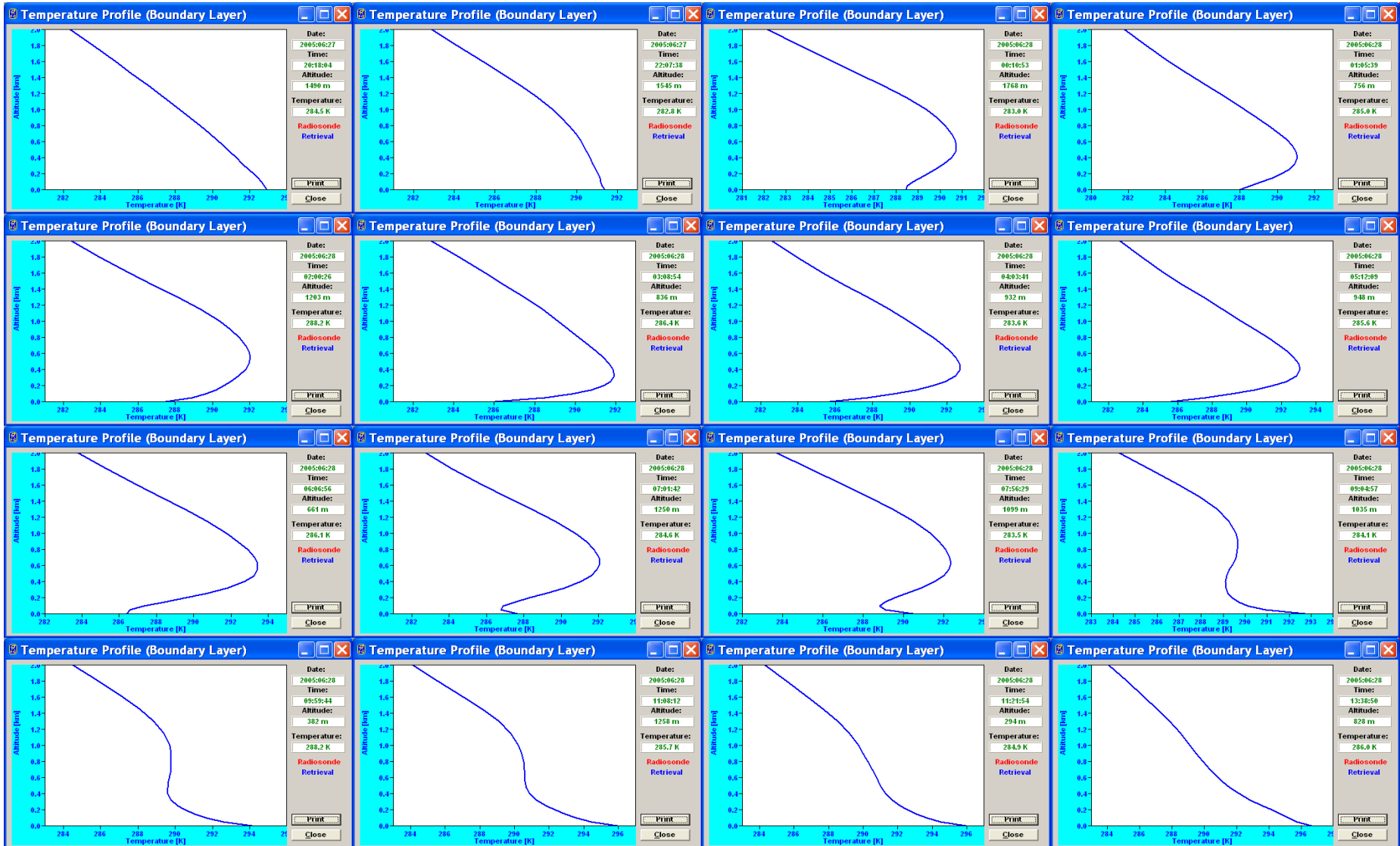
140 radio soundings (26. April to 4. July, Cabauw, KNMI).

Radiosonds: Vaisala RS-92.

No-Rain RMS: **0.43 kg/m<sup>2</sup>, Bias: 0.05 kg/m<sup>2</sup>**



# Time series of temperature inversion



*Thank you!*

`czekala@radiometer-physics.de`